



*Fundamentals of synoptic meteorology*

*Lecture 16*

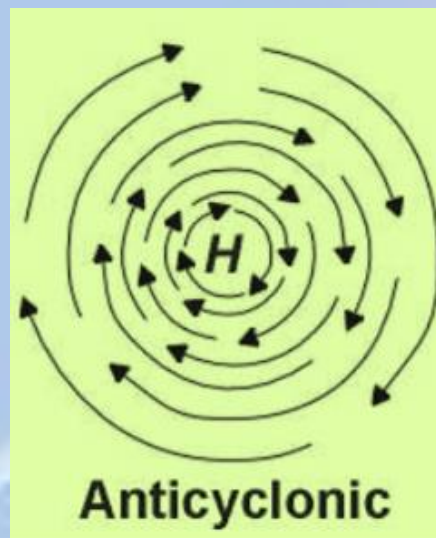
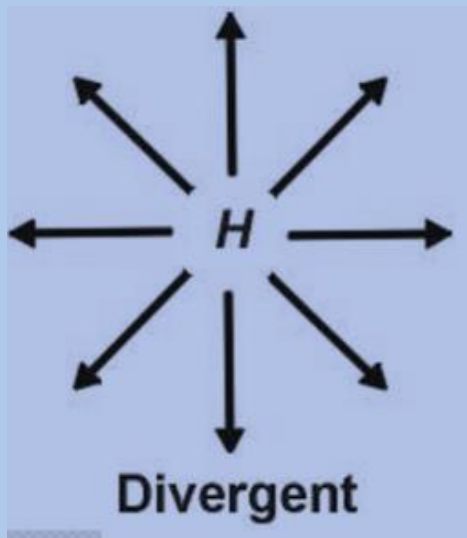
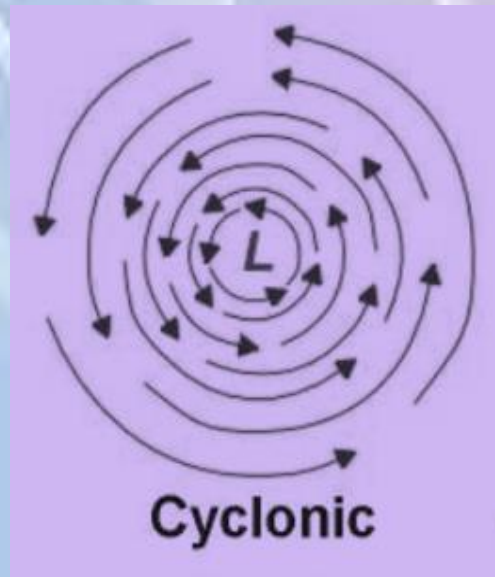
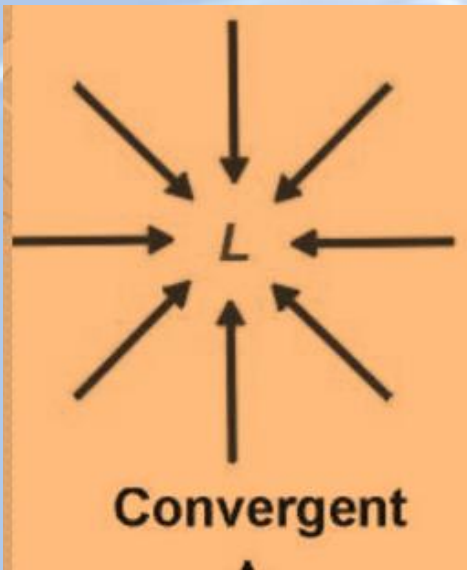
*Physics Department*

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*Sahraei*

*<http://www.razi.ac.ir/sahraei>*

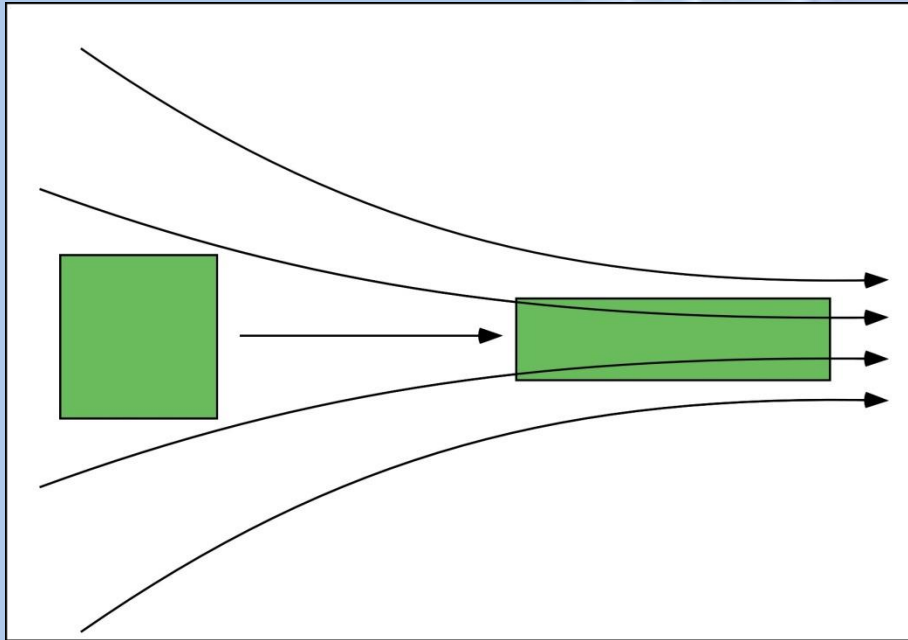
# Examples of Flow



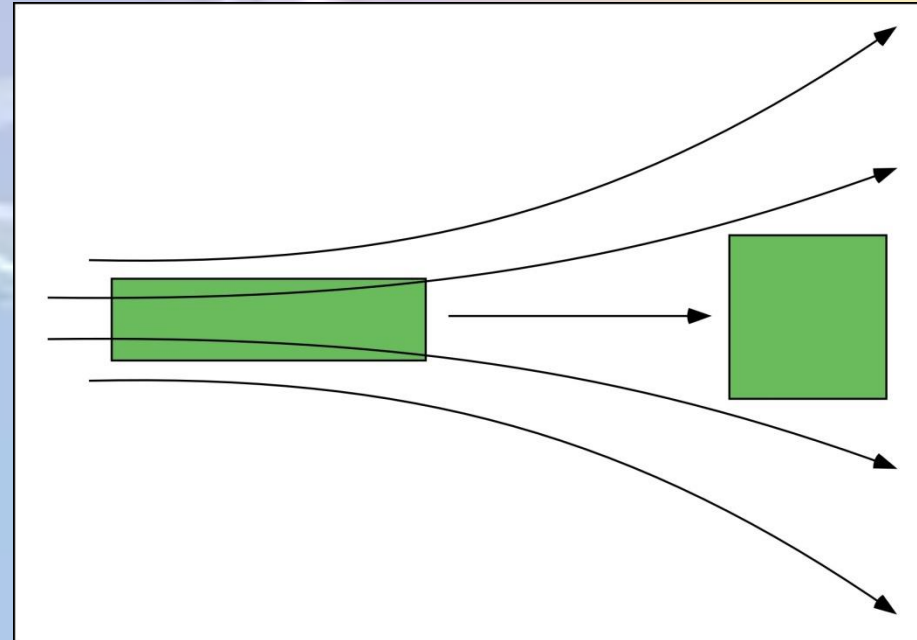


## CONFLUENT and DIFLUENT FLOW

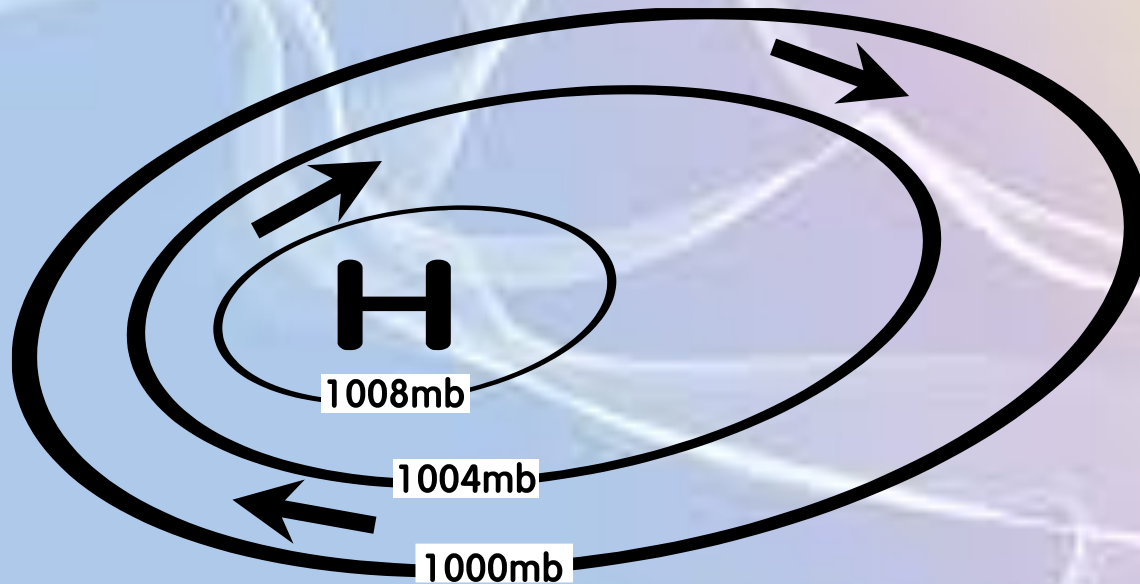
Is this flow convergent?



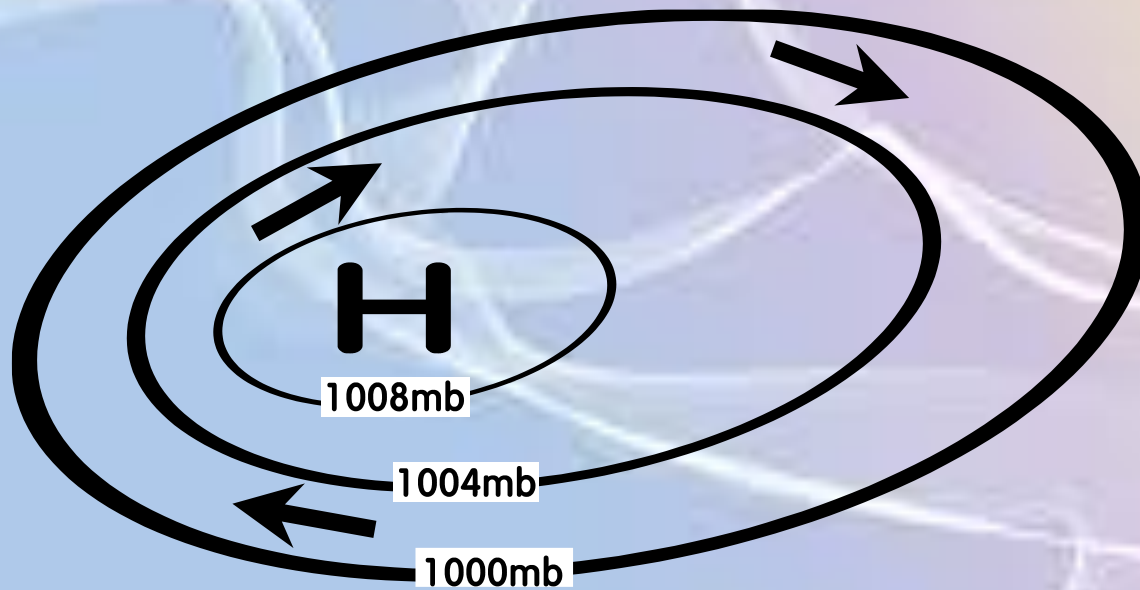
Is this flow divergent?



NO: The areas of the two boxes are identical  
The flow is a combination of translation and deformation

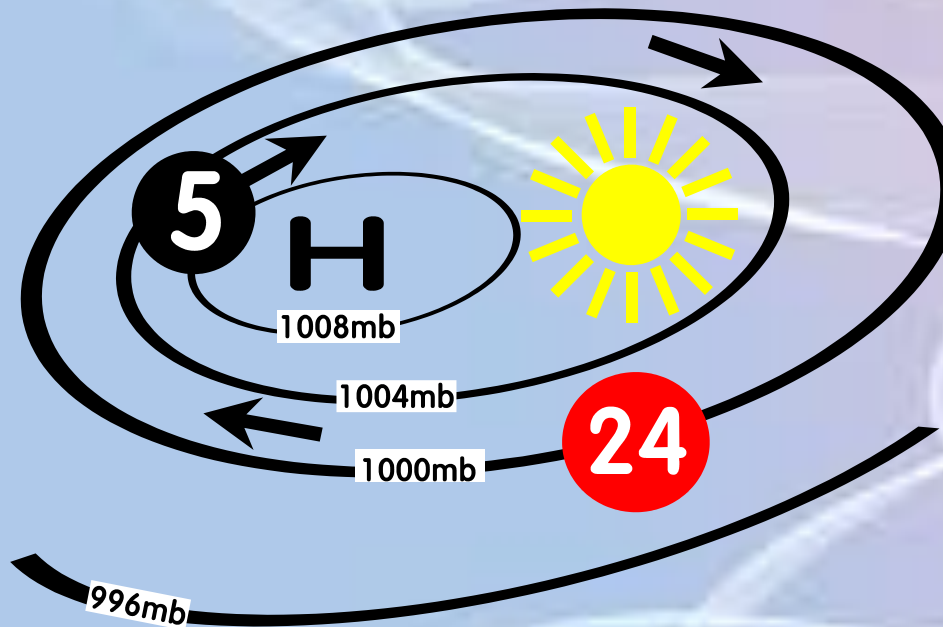


**an anti-cyclone  
has high pressure,  
and clockwise winds**

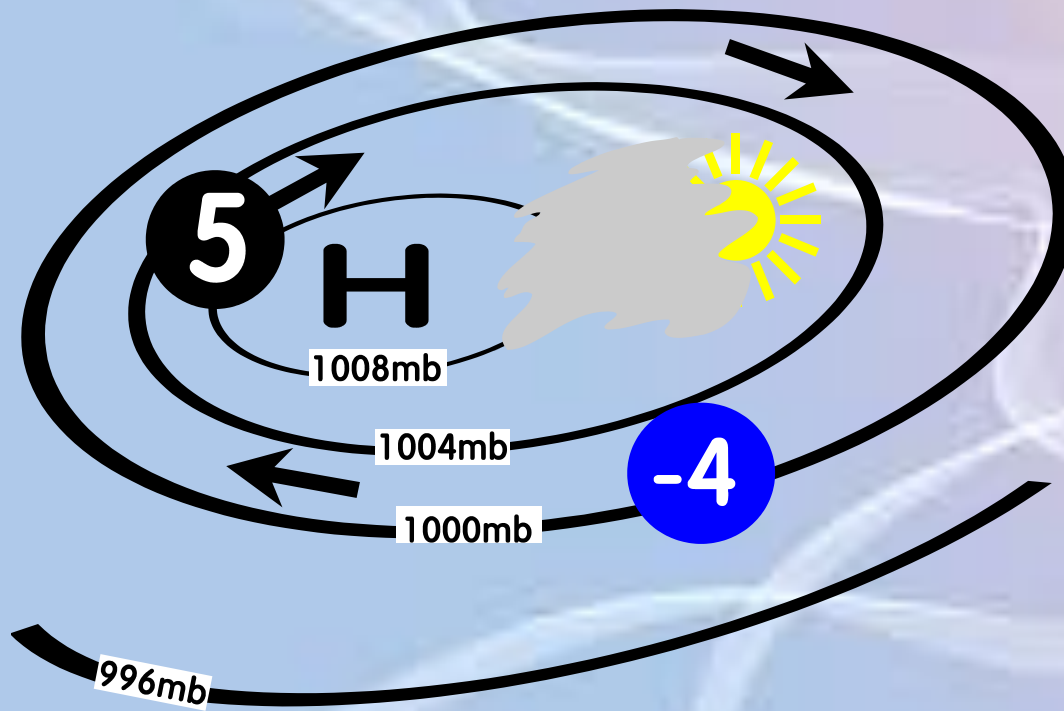


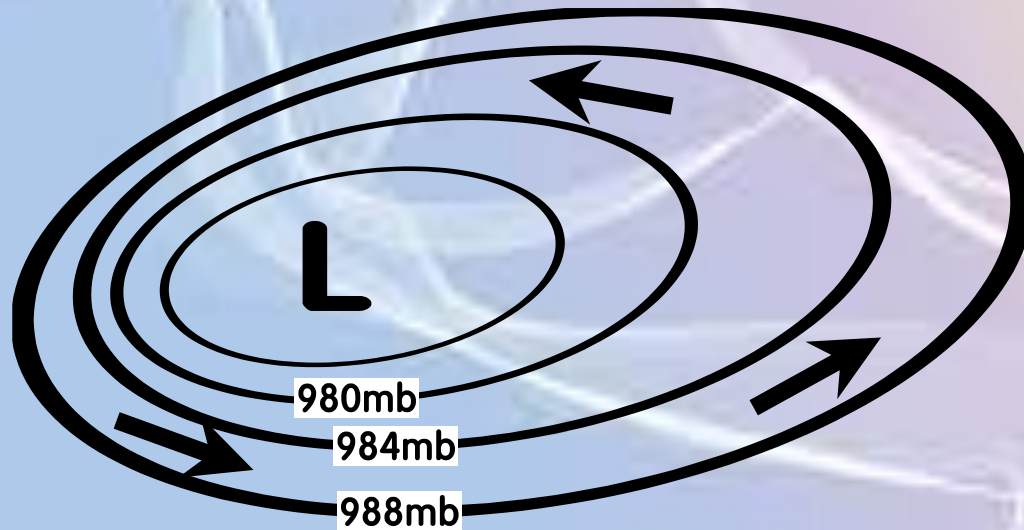
**an anti-cyclone  
has widely spaced isobars  
and gentle winds**

high pressure in summer  
gives hot, settled, sunny  
weather with gentle winds



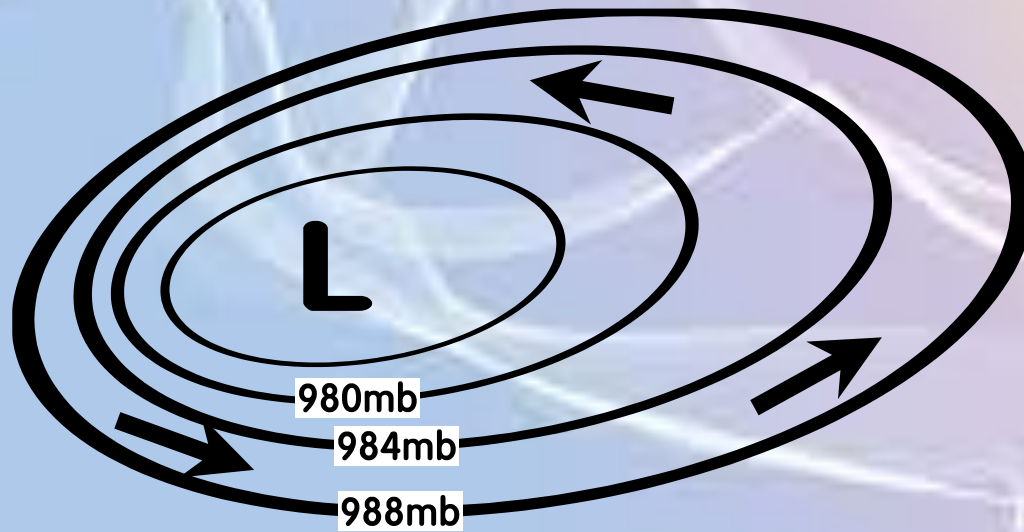
high pressure in winter  
gives very cold, settled  
weather with gentle winds,  
frost and possible fog.



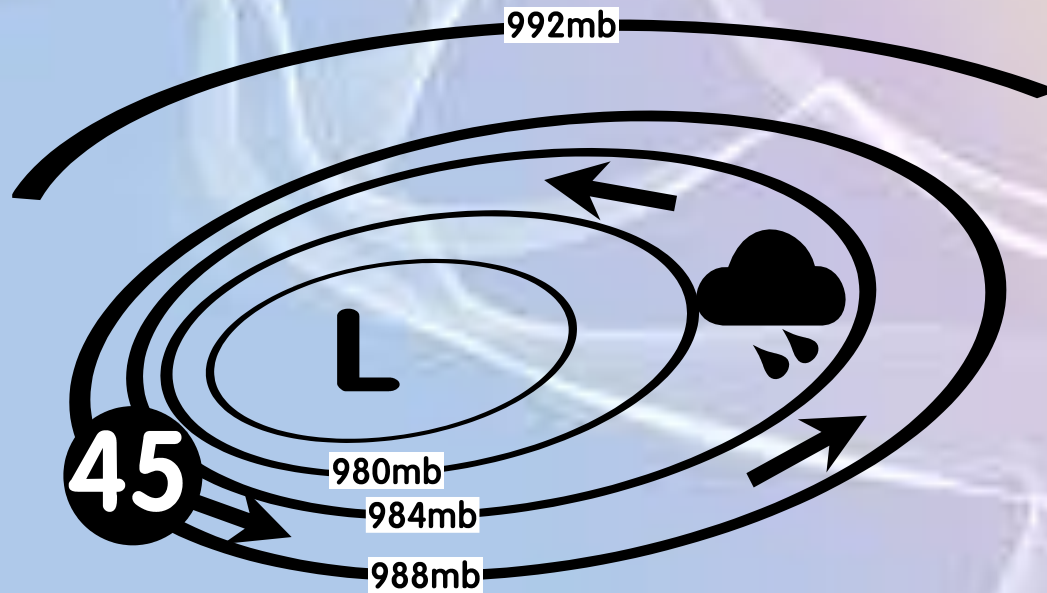


**a cyclone or depression  
has low pressure,  
and anti-clockwise winds**



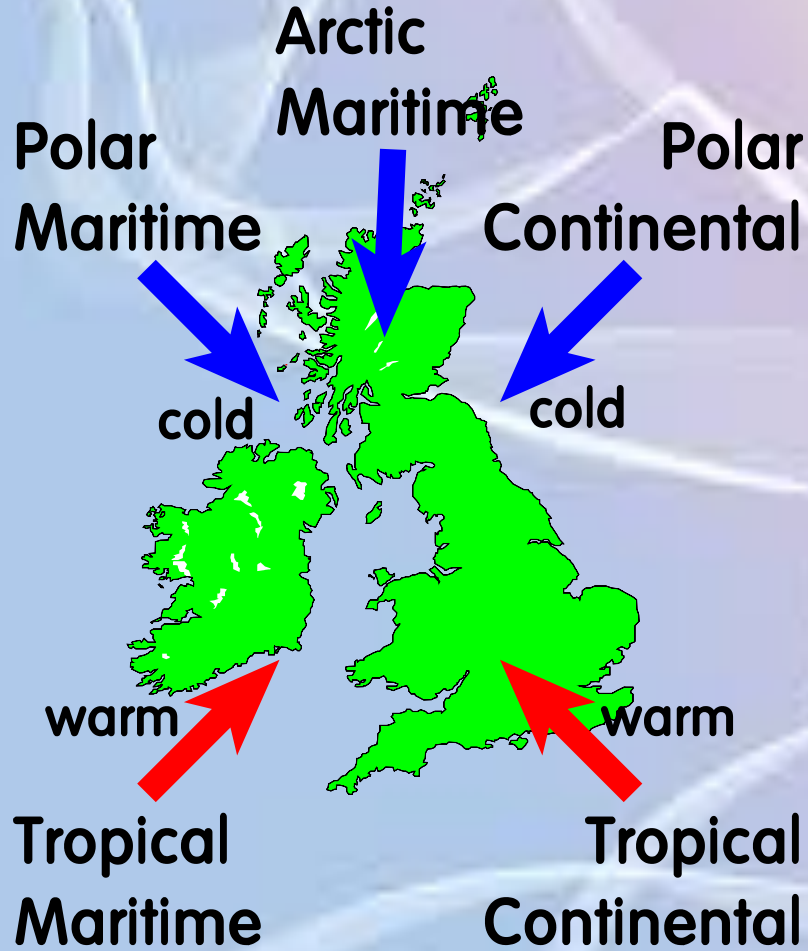


**a cyclone has tightly  
packed isobars  
and strong winds**

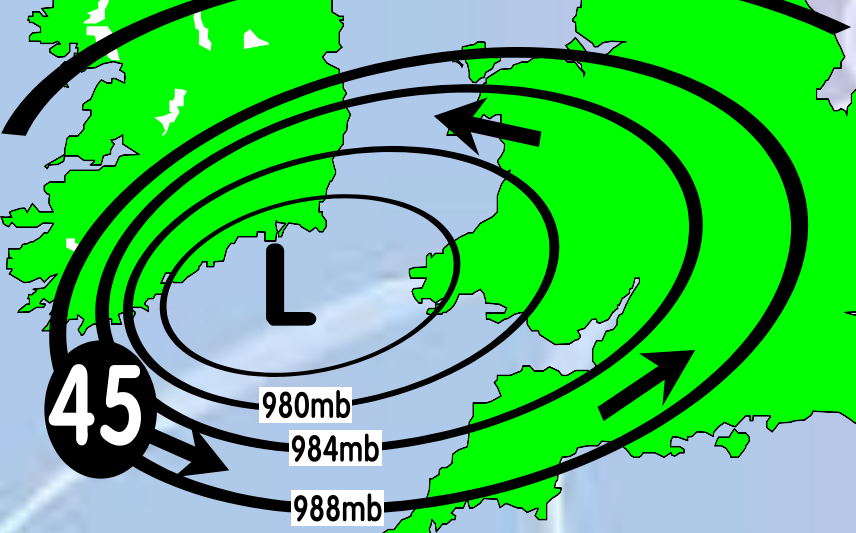
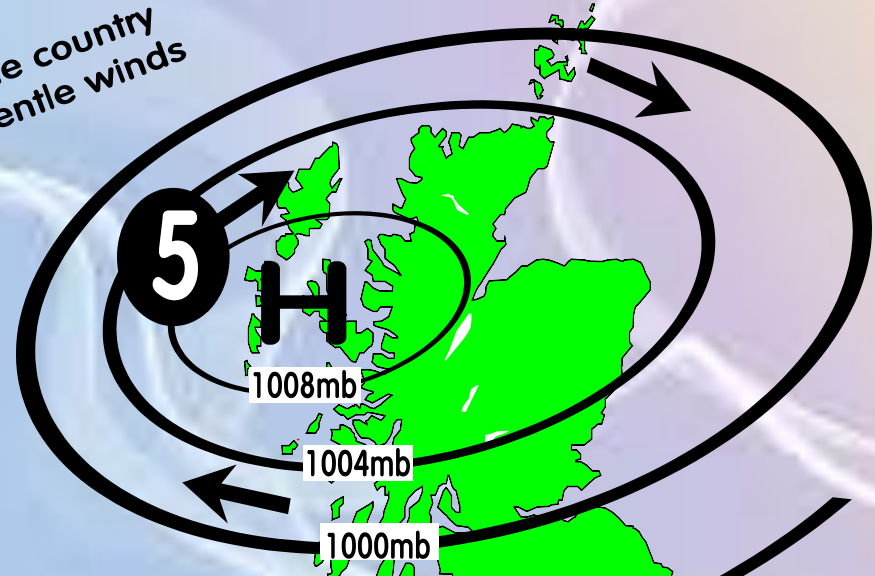


low pressure areas at  
any time of year give wet  
weather with strong winds

# Air Masses which affect British Weather



high pressure to the North of the country  
means settled weather with gentle winds



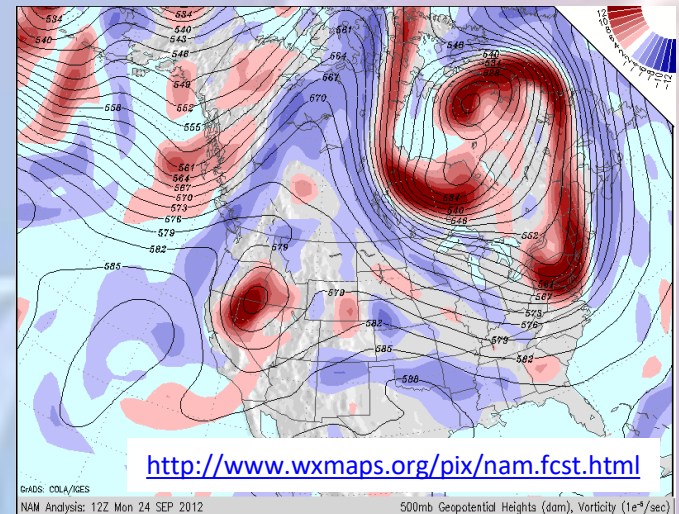
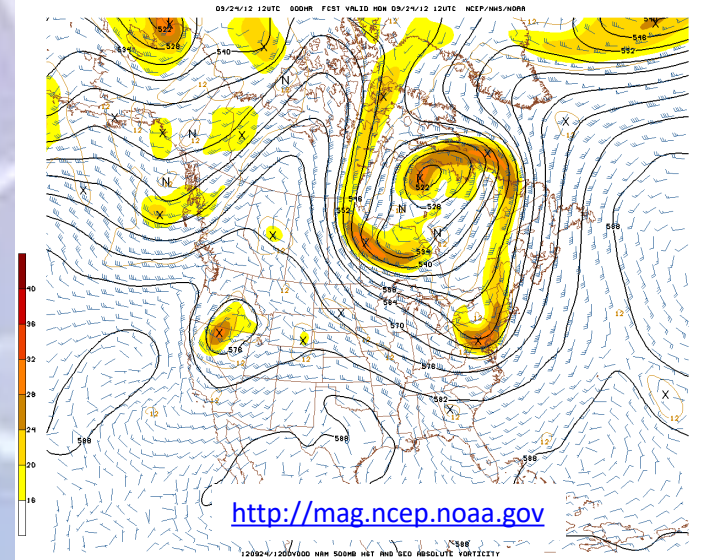
low pressure to the South  
of the country means wet  
weather with strong winds



# What is vorticity?

Many meteorological web sites include some form of vorticity contours on the 500-mb charts

Why? How does having contours of vorticity help a meteorologist understand the atmosphere?



## *vorticity*

Vorticity is a measure of local spin

$$\vec{\omega} = \nabla \times \vec{V} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ u & v & w \end{vmatrix} = \hat{i} \left( \frac{\partial w}{\partial y} - \frac{\partial v}{\partial z} \right) + \hat{j} \left( \frac{\partial u}{\partial z} - \frac{\partial w}{\partial x} \right) + \hat{k} \left( \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \right)$$

On a weather chart (like the 500 mb chart), want to measure spin about a vertical axis

So isolate the "vertical vorticity"  $\zeta$  :

This quantity is also often called "relative vorticity"

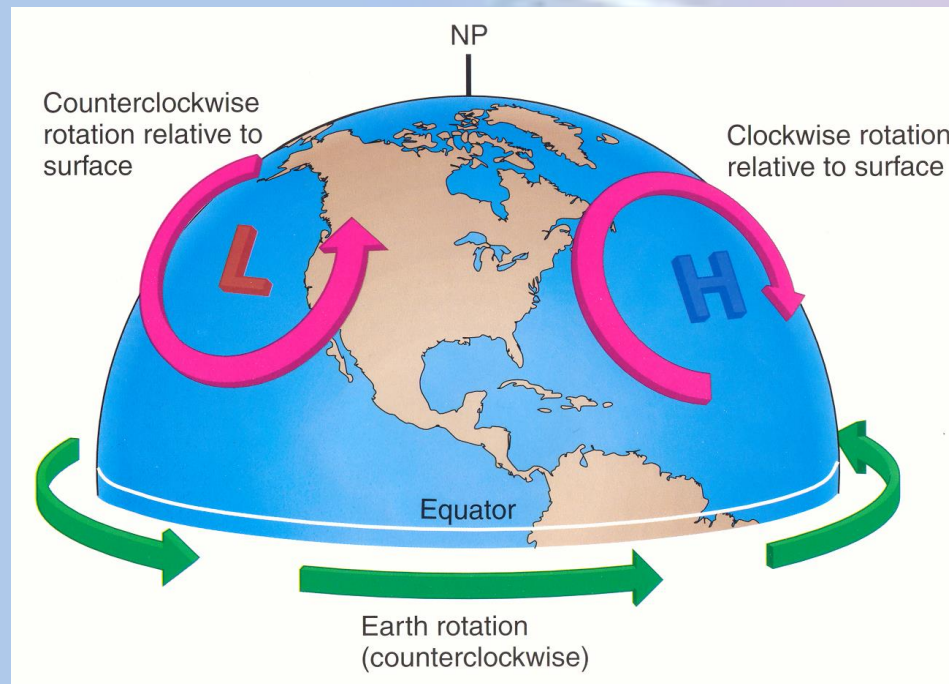
$$\zeta = \left( \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \right)$$

## Relative vorticity

Relative (vertical) vorticity is not a measure of “vertical spin”, but rather a measure of *horizontal spin*.

The word “vertical” comes from the fact that it’s the  $\hat{k}$  component of the vorticity vector.

**Advantage:** in one variable, both  $u$  and  $v$  wind components are used



## *vorticity sources*

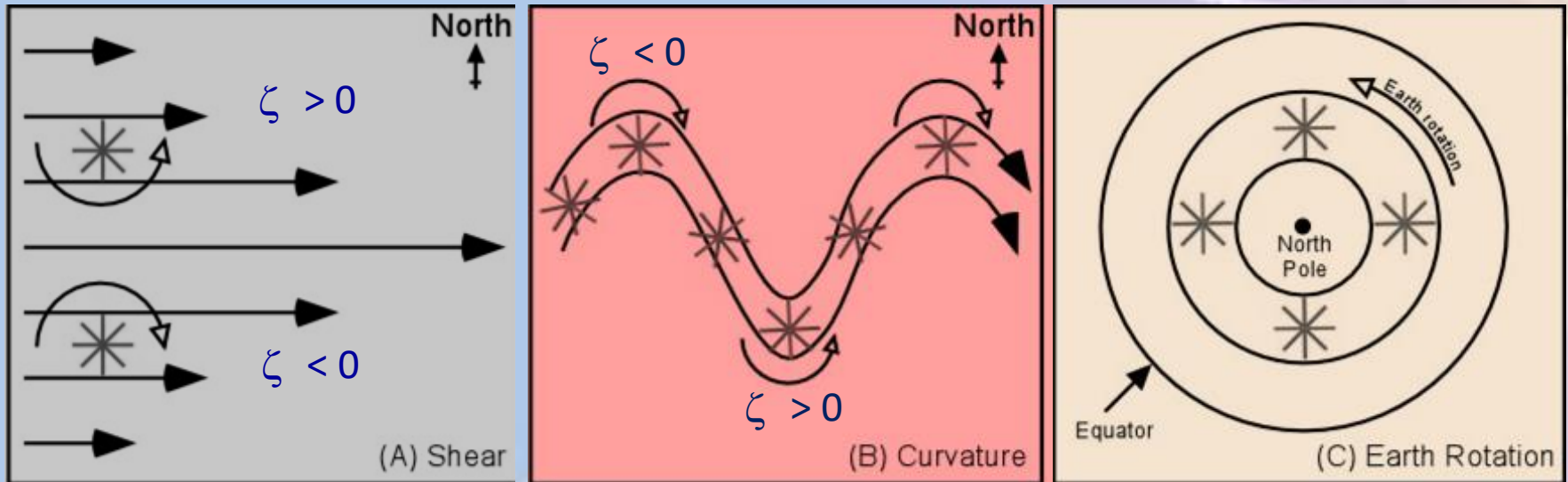
Vertical vorticity (spin about a vertical axis) arises from three sources: Horizontally sheared flow, flow curvature, and the rotation of the earth.

Relative vorticity: shear and curvature.

$$\zeta = \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y}$$

Absolute vorticity: shear, curvature and earth rotation.  $\zeta_a = \zeta + f$

### *Sign convention*



The earth would spin counter-clockwise if you looked down on it from above the north pole



Relative vorticity is non-zero for two reasons:

$$\zeta = \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y}$$

Either streamlines of wind have curvature, or

The wind field has horizontal shear (or both)

## Earth's vorticity

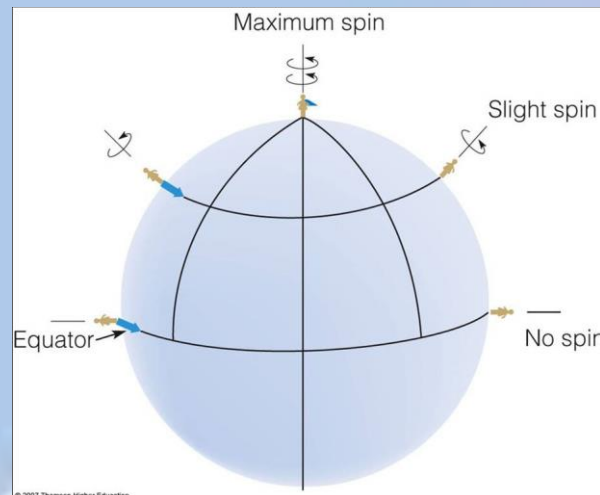
The Earth is a rotating sphere.

It imparts vorticity to fluid parcels

Earth vorticity along the vertical axis is called Coriolis:

$f = 2\Omega \sin \theta$ , where  $f$  is Coriolis parameter,  $\Omega$  is the angular speed of earth's rotation, and  $\theta$  is latitude

In Southern Hemisphere, Earth's vorticity is negative (why?)



Typical magnitude of the relative vorticity for synoptic scale flow,

$U \sim 10 \text{ m/s},$

$L \sim 1000 \text{ km}$

$$\zeta \approx \frac{U}{L} = 10^{-5} \text{ s}^{-1}$$

Typical magnitude of planetary vorticity  $f \sim 10^{-4} \text{ s}^{-1}$

## *Geostrophic absolute vorticity*

To examine the actual spin of an air parcel, need to look at vorticity contributions from both the Earth and the parcels themselves:

Absolute vorticity:  $\zeta_a = \zeta + f$

At 500 mb, flow is nearly geostrophic

So re-name relative vorticity as "geostrophic relative vorticity"  $\zeta_g$

Also re-name absolute vorticity as "geostrophic absolute vorticity"

$$\zeta_{ga} = \zeta_g + f$$



Geostrophic relative vorticity: average difference in geopotential height around a central point.

If average height is higher across the region than at the center point, geostrophic vorticity is positive (i.e. cyclonic)

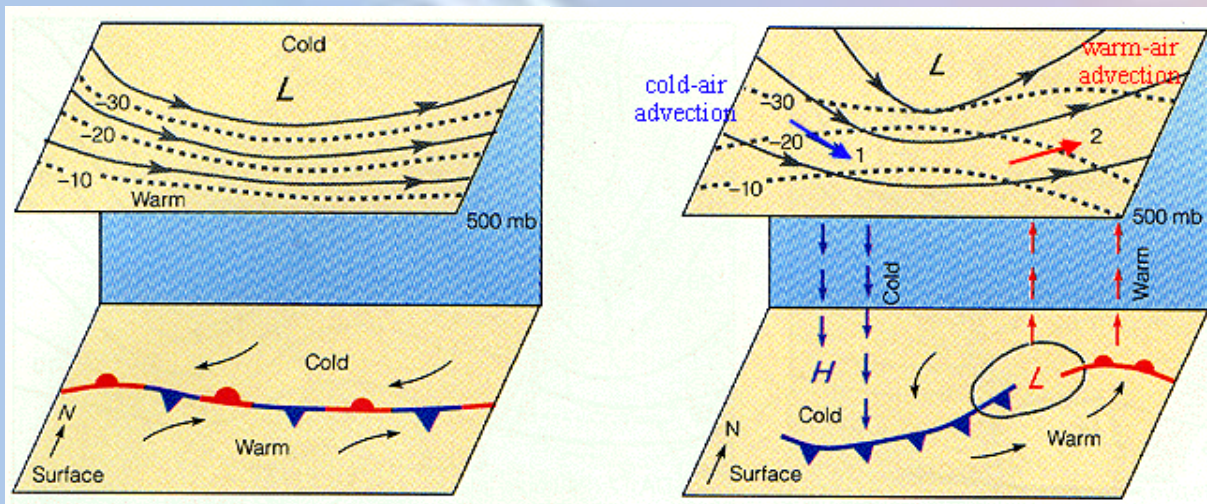
i.e., point is lower than its surroundings, such as in a trough

If average height is lower than at center point, geostrophic vorticity is negative (i.e., anticyclonic)

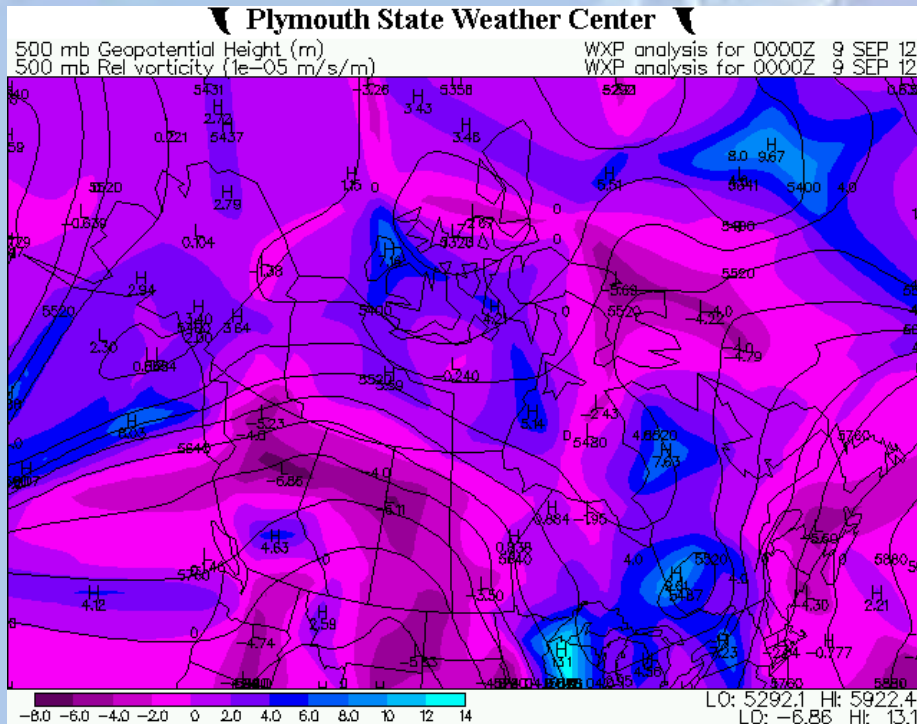
i.e., point is higher than its surroundings, such as in a ridge

# Importance of vorticity

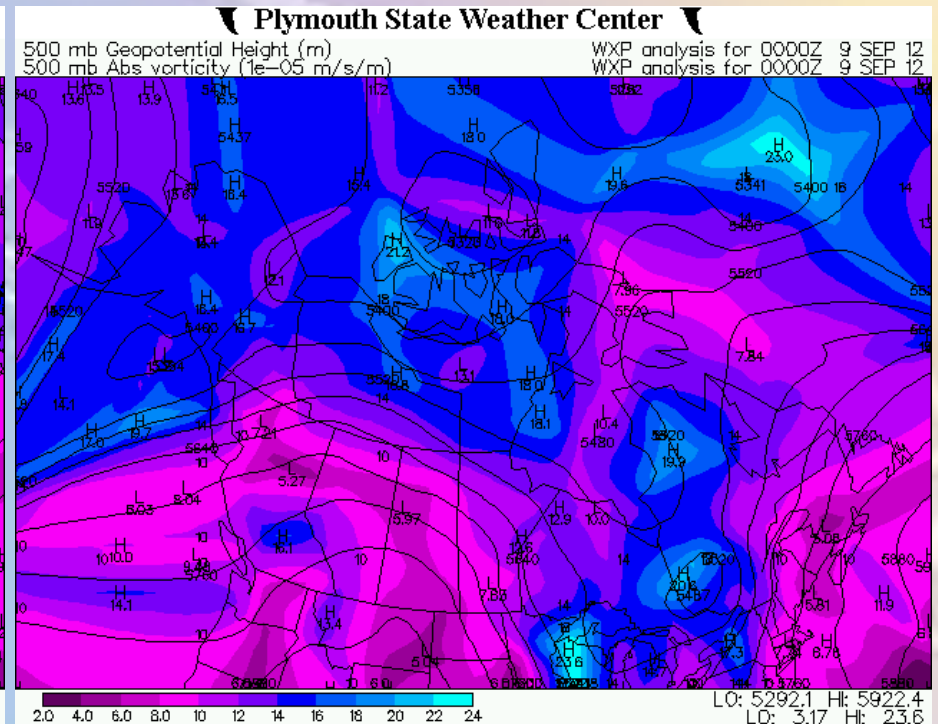
vorticity is the quantity that "spins up" (or down) during the development of an extratropical cyclone



# Relative & absolute vorticity in higher latitudes (Canada)



500 mb Geopotential Height (m)  
500 mb Rel vorticity ( $1e-05$  m/s/m)



500 mb Geopotential Height (m)  
500 mb Abs vorticity ( $1e-05$  m/s/m)

Note color scale differences

## *Why Care about Upper-Air?*

Talked about surface pressure and what winds we expect to see at the surface

Lots of atmosphere not at the surface that affects weather conditions at the surface!

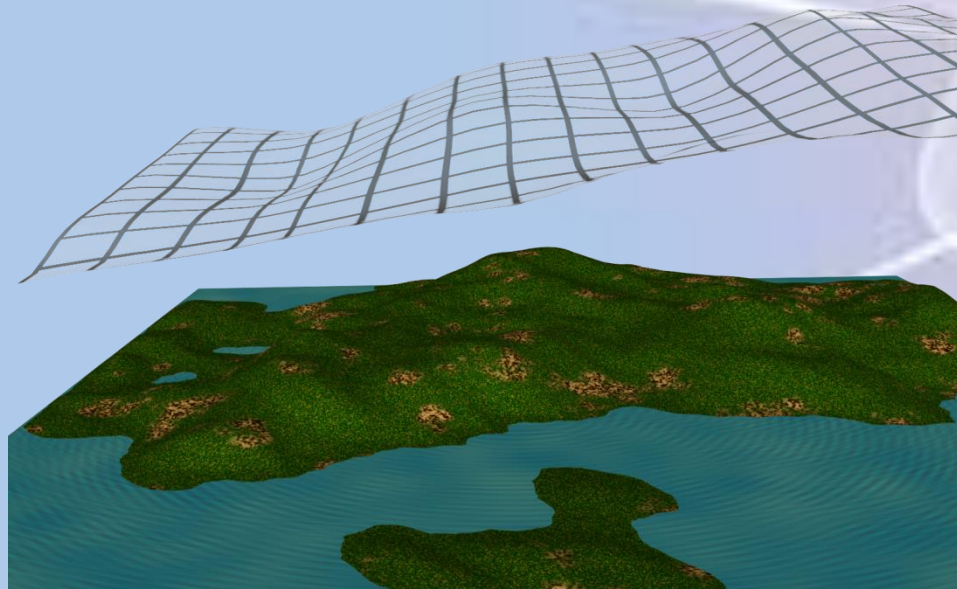
Need to have ways to observe and analyze the atmosphere kilometers from the surface



## Maps of weather above the surface

Upper-air weather conditions plotted on maps of constant pressure.

Data obtained from radiosondes: heights, temperatures, wind speeds and directions, humidity



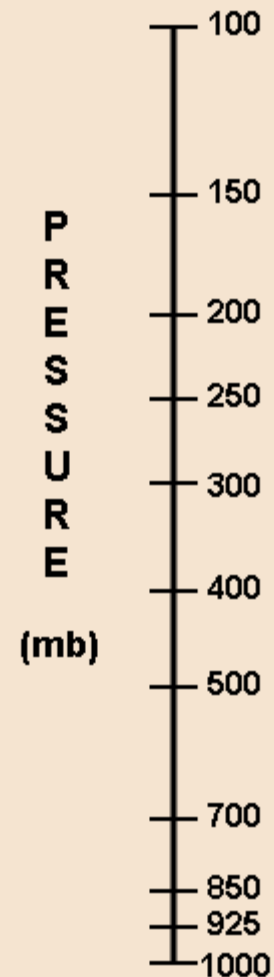
# *Constant Pressure Surfaces*

Simplifies math

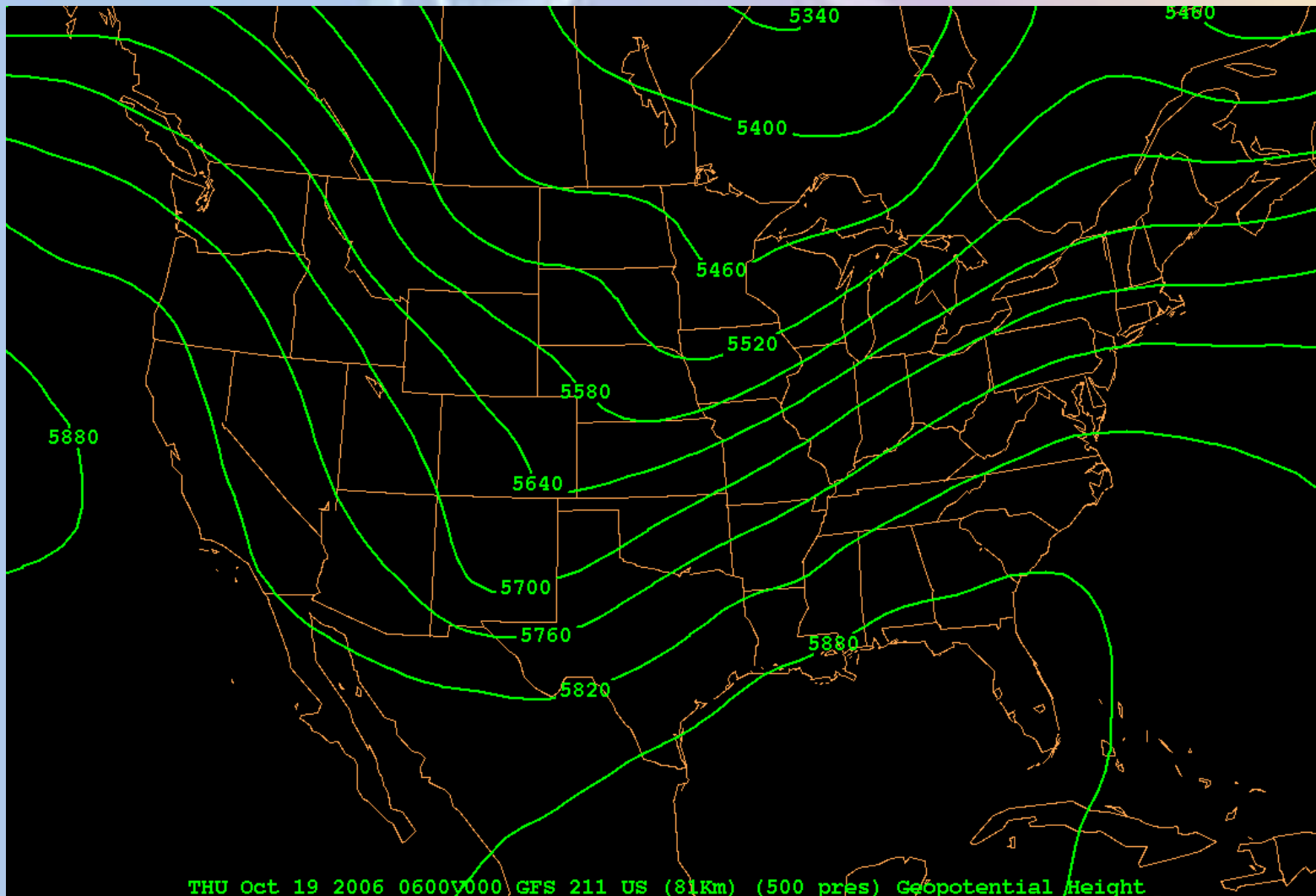
All upper-air maps plotted on constant pressure surfaces.

Mandatory pressure levels: pressures where radiosondes always take observations.

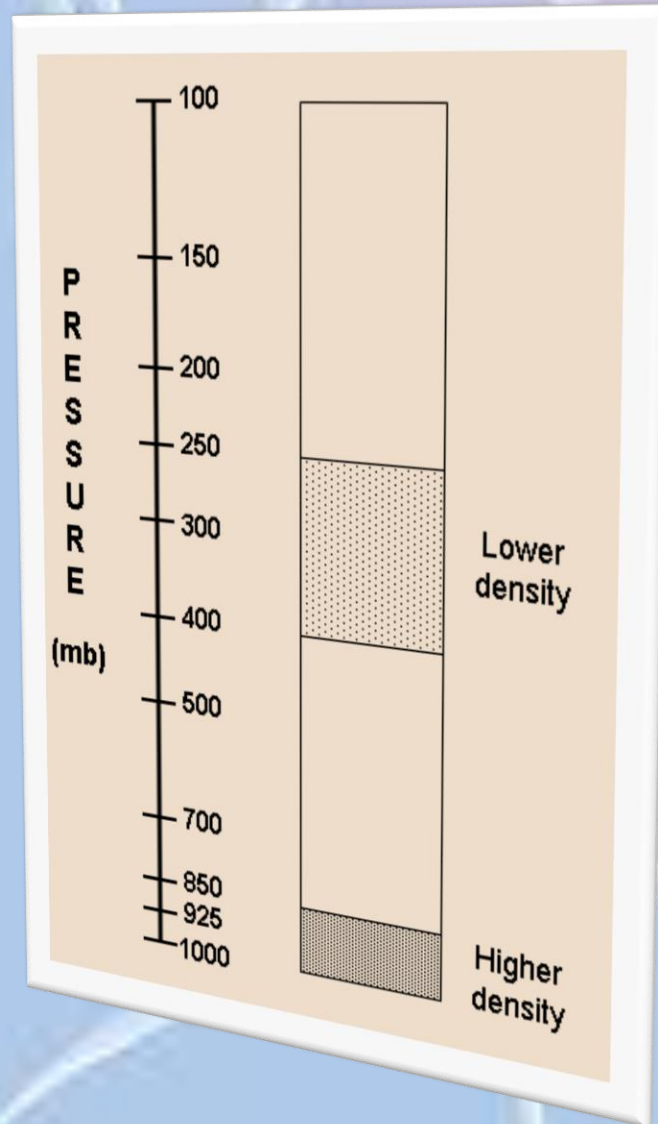
Pressure decreases faster with height closer to ground.



*A 500 mb chart*  
*Height contours, isohypses, or heights*  
*(isopleths of equal height)*

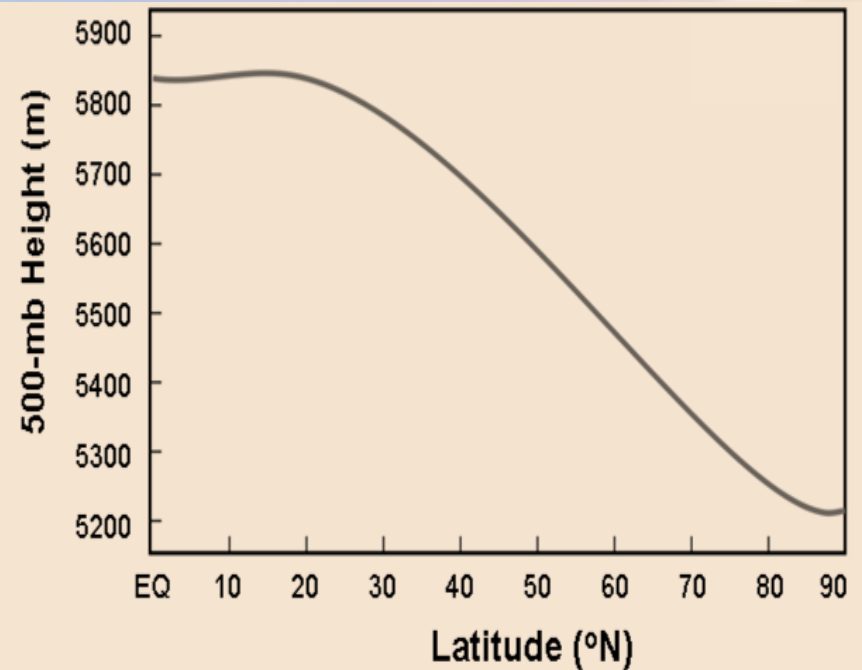
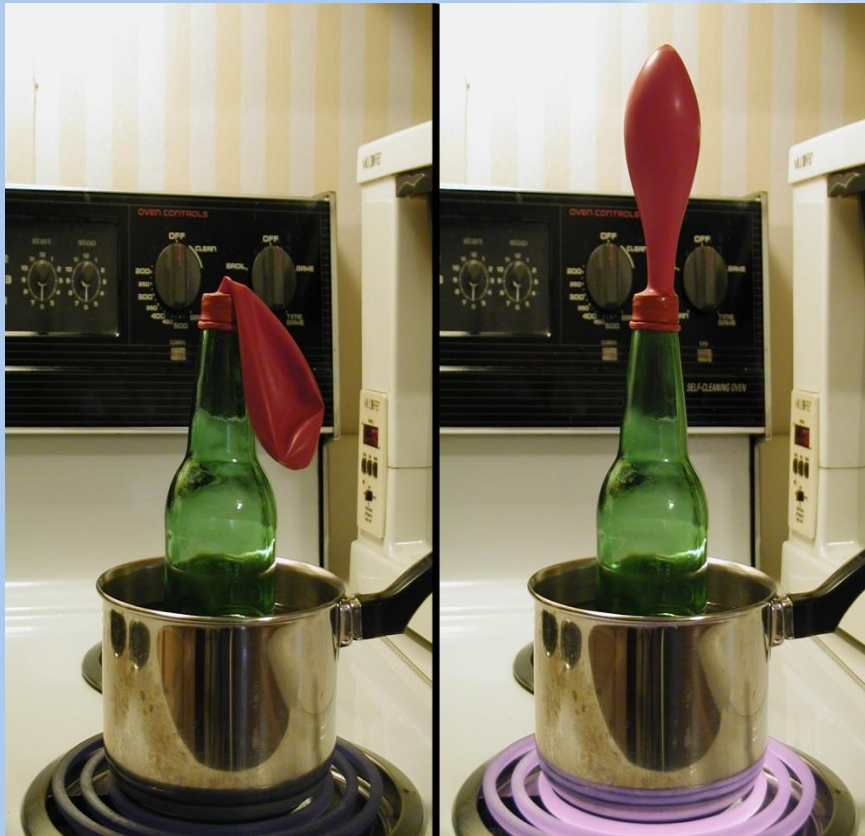


# Density decreases with height



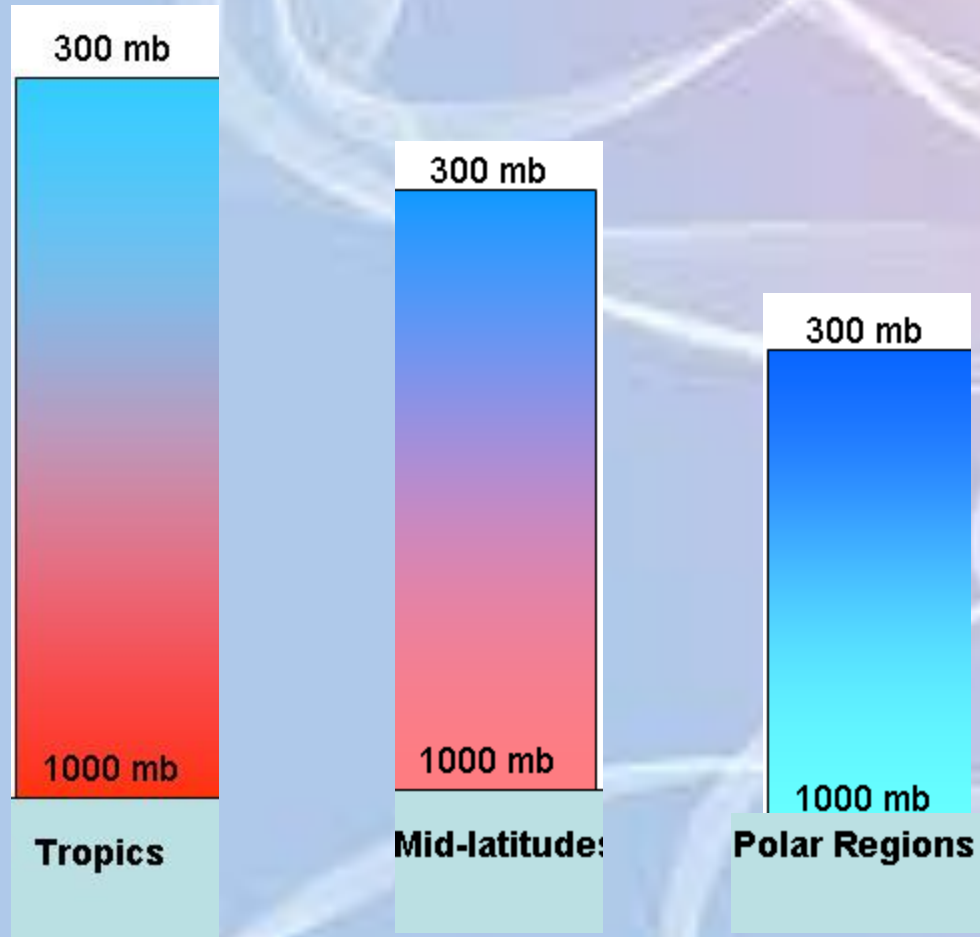
A volume of air will become larger when heated

Pressure decreases more rapidly with height in cold air columns than warm air columns





Warm columns of air taller than cold columns



## Forming upper-level troughs/ridges

Cold air masses move south, warm air masses move north...forming upper-level troughs/ridges

