## General Meteorology

Lecture 8


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## Applications of Clausius-Clapeyron Equation

$$
\frac{d e_{s}}{d T}=\frac{L_{12}}{\left(\alpha_{2}-\alpha_{1}\right) T}
$$



$$
\frac{d e_{s}}{d T}=\frac{\mathrm{L}_{\mathrm{w} v}}{T\left(\alpha_{v}-\alpha_{w}\right)}
$$

$$
\frac{d e_{s}}{d T}=\frac{L_{i v}}{T\left(\alpha_{v}-\alpha_{i}\right)}
$$

$$
\frac{d e_{s}}{d T}=\frac{L_{\mathrm{iw}}}{T\left(\alpha_{w}-\alpha_{i}\right)}
$$

## Water in Equilibrium

## Three Standard Equilibrium States:

Vaporization: Gas $\leftrightarrow$ Liquid
Fusion: $\quad$ Liquid $\leftrightarrow$ Ice
Sublimation: Gas $\leftrightarrow$ Solid

- Each of these equilibrium states occur at certain temperatures and pressure
- Thus we can construct an equilibrium phase change graph for water


Provides the mathematical relationship (i.e., the equation) that describes any equilibrium state of water as a function of temperature and pressure.

## Water in Equilibrium

## One Unique Equilibrium State:

- It is possible for all three phases to co-exist in an equilibrium at a single temperature and pressure
- Called the Triple Point

$$
\begin{aligned}
& p_{v}=p_{w}=p_{i} \\
& T_{v}=T_{w}=T_{i} \\
& p=6.11 \mathrm{mb} \\
& T=273.16 \mathrm{~K}
\end{aligned}
$$

## Water in Equilibrium

## Critical Point:

- Thermodynamic state in which liquid and gas phases can co-exist in equilibrium at the highest possible temperature

$$
\begin{gathered}
T_{c}=374^{\circ} \mathrm{C} \\
p_{c}=221,000 \mathrm{mb}
\end{gathered}
$$

- Above this temperature, water can NOT exist in the liquid phase


## Other Atmospheric Gases:

$$
\mathrm{O}_{2} \quad \rightarrow \quad T_{c}=-119^{\circ} \mathrm{C}
$$

$$
N_{2} \quad \rightarrow \quad T_{c}=-147^{\circ} \mathrm{C}
$$



$$
\mathrm{CO}_{2} \quad \rightarrow \quad T_{c}=31^{o} \mathrm{C}
$$

## Computing saturation vapor pressure for a given temperature:

Version 1: Assumes constant latent heat of vaporization ( $L=$ constant) Less accurate at extreme temperatures

$$
\begin{gathered}
\frac{d e_{s}}{d T}=\frac{L_{w v}}{\left(\alpha_{v}-\alpha_{L}\right) T} \quad e_{s} \alpha_{v}=R_{v} T \\
\frac{d e_{s}}{d T}=\frac{L_{w v} \mathrm{e}_{s}}{R_{v} T^{r}}
\end{gathered}
$$

$$
\left.e_{s w}(m b)=6.11 \exp \left[\frac{L}{R_{v}}\left(\frac{1}{273.15}-\frac{1}{T(K)}\right)\right)\right\rfloor
$$

## Saturated Adiabatic Lapse Rate

## Temperature Changes Inside Clouds

Two processes occur simultaneously inside clouds that affect the temperature.
(1) Rising air expands, does work and cools;
(2) Condensation releases latent energy which is then stored as internal energy and warms the air inside the cloud.

Normally, the cooling due to the work of expansion is greater than the warming associated with the release of latent energy and its conversion to internal energy.

Thus, as air rises inside a cloud it still gets colder, but it does so at a slower rate than the Dry Adiabatic Lapse rate.

The rate at which rising air inside a cloud cools is called the Saturated Adiabatic Lapse Rate (SALR).

## The Saturated Adiabatic Lapse Rate (SALR)

The derivation of the equation for the SALR begins with a form of the First Law of Thermodynamics

$$
d q=c_{p} d T-\alpha d p
$$

In this case the energy gained, dq , is equal to the latent energy released when water vapor condenses inside the cloud.
where

$$
d q=-L_{v w} d q_{\mathrm{v}} \quad q=\frac{m_{v}}{m_{v}+m_{d}}
$$

$L_{w v}$ is the latent heat of vaporization, and
$d q_{v}$ is the change of specific humidity of the air parcel when water vapor condenses

Substitute for dq in the First Law of thermodynamics to get

$$
-L_{\mathrm{vw}} d q_{\mathrm{v}}=c_{p} d T-\alpha d p
$$

Add $-c_{p} d T+L_{v w} d q_{v}$ to both sides to get

$$
-c_{p} d T=-a d p+L_{v w} d q_{v}
$$

Divide by $c_{p} d z$ to get
$\frac{-c_{p} d T}{c_{p} d z}=\frac{-a d p}{c_{p} d z}+\frac{L_{v w} d q_{v}}{c_{p} d z} \quad \frac{-d T}{d z}=\frac{-d p}{c_{p} \rho d z}+\frac{L_{v w} d q_{v}}{c_{p} d z}$
Since $a=1 / \rho$

$$
g=\frac{-d p}{\rho d z}
$$

$$
\frac{-d T}{d z}=\frac{\mathrm{g}}{c_{p}}+\frac{L_{v w} d q_{v}}{c_{p} d z}=\Gamma_{\mathrm{s}}
$$

$S A L R=$| cooling due |
| :--- |
| to work of |
| expansion |$+$| warming due to |
| :--- |
| latent energy |
| released during |
| condensation |

The SALR is always less than the DALR because the cooling caused by adiabatic expansion is partially offest by the release of latent energy during condensation.

The SALR is a variable.
The magnitude of the SALR is determined by the amount of water vapor that condenses.

## Moist Adiabatic Rate



LCL: the level in the atmosphere at which an unsaturated air parcel lifted dry adiabatically would become saturated.

